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#1 HOME TUITION AGENCY

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**Cambridge International Examinations**  
Cambridge International General Certificate of Secondary Education

CANDIDATE  
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CENTRE  
NUMBER

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CANDIDATE  
NUMBER

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**ADDITIONAL MATHEMATICS**

**0606/11**

Paper 1

**October/November 2016**

**2 hours**

Candidates answer on the Question Paper.

Additional Materials:      Electronic calculator

**READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.  
Write in dark blue or black pen.  
You may use an HB pencil for any diagrams or graphs.  
Do not use staples, paper clips, glue or correction fluid.  
**DO NOT WRITE IN ANY BARCODES.**

Answer **all** the questions.  
Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.  
The use of an electronic calculator is expected, where appropriate.  
You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.  
The number of marks is given in brackets [ ] at the end of each question or part question.  
The total number of marks for this paper is 80.

This document consists of **16** printed pages.

## Mathematical Formulae

### 1. ALGEBRA

#### Quadratic Equation

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}.$$

#### Binomial Theorem

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1} b + \binom{n}{2} a^{n-2} b^2 + \dots + \binom{n}{r} a^{n-r} b^r + \dots + b^n,$$

where  $n$  is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$ .

### 2. TRIGONOMETRY

#### Identities

$$\sin^2 A + \cos^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A$$

#### Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2} bc \sin A$$

1 (a) Sets  $\mathcal{C}$ ,  $A$  and  $B$  are such that

$$n(\mathcal{C}) = 26, n(A \cap B') = 7, n(A \cap B) = 3 \text{ and } n(B) = 15.$$

Using a Venn diagram, or otherwise, find

(i)  $n(A)$ , [1]

(ii)  $n(A \cup B)$ , [1]

(iii)  $n(A \cup B)'$ . [1]

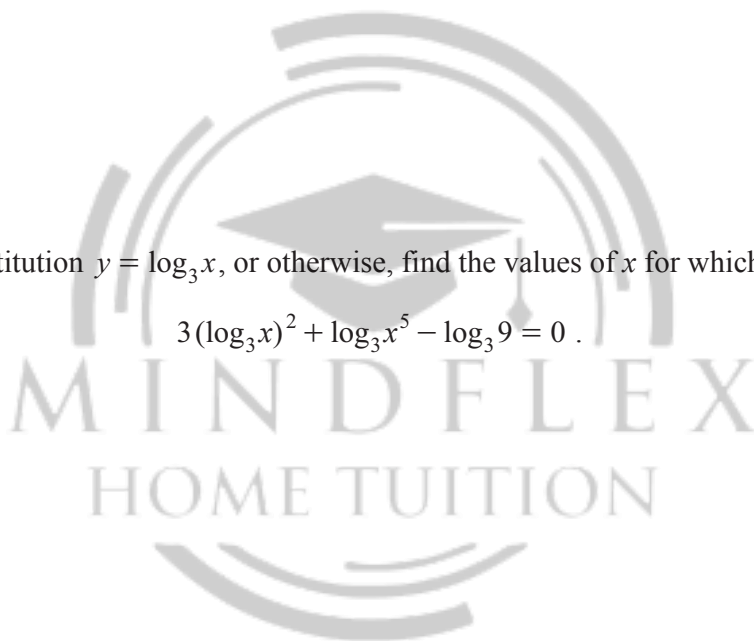
(b) It is given that  $\mathcal{C} = \{x : 0 < x < 30\}$ ,  $P = \{\text{multiples of } 5\}$ ,  $Q = \{\text{multiples of } 6\}$  and  $R = \{\text{multiples of } 2\}$ . Use set notation to complete the following statements.

(i)  $Q \dots\dots\dots R$ , [1]

(ii)  $P \cap Q = \dots\dots\dots$  [1]

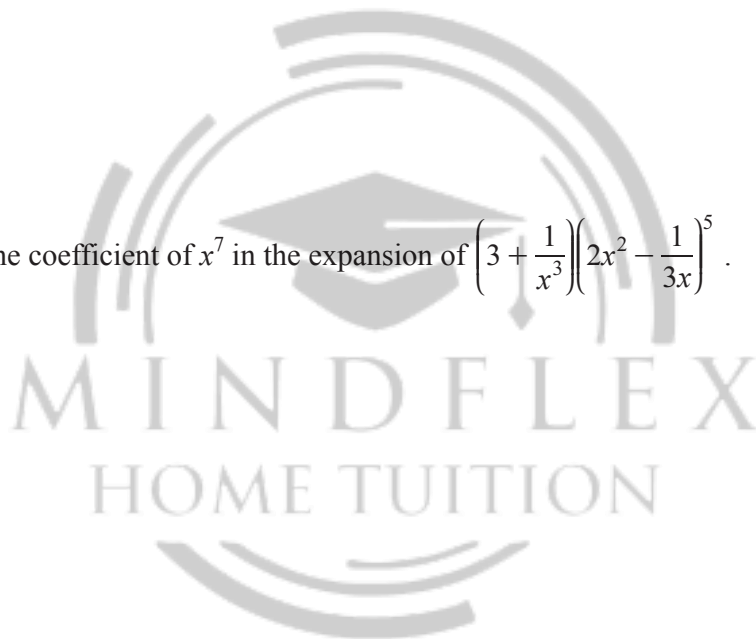
2 Given that  $\frac{p^{\frac{1}{3}}q^{-\frac{1}{2}}r^{\frac{3}{2}}}{p^{-\frac{2}{3}}\sqrt{(qr)}^5} = p^a q^b r^c$ , find the value of each of the integers  $a$ ,  $b$  and  $c$ . [3]

3 By using the substitution  $y = \log_3 x$ , or otherwise, find the values of  $x$  for which  $3(\log_3 x)^2 + \log_3 x^5 - \log_3 9 = 0$ . [6]



- 4 (i) Find the first 3 terms in the expansion of  $\left(2x^2 - \frac{1}{3x}\right)^5$ , in descending powers of  $x$ . [3]

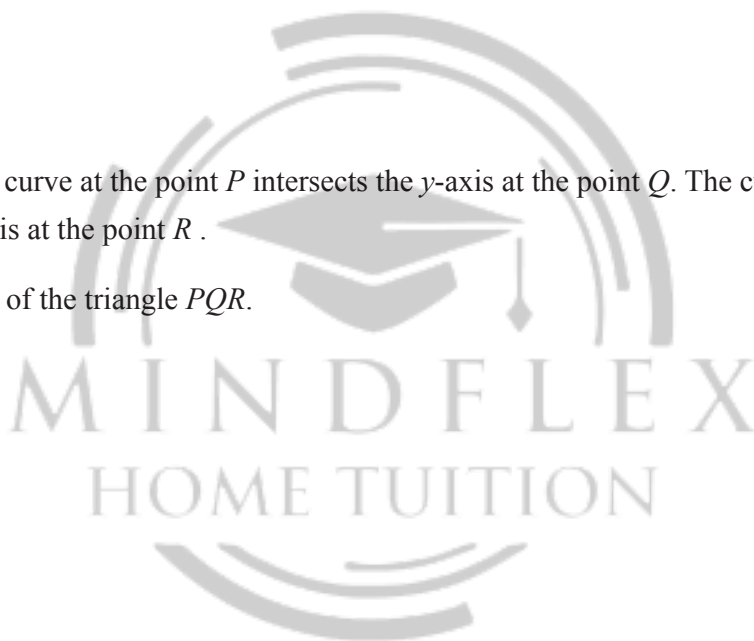
- (ii) Hence find the coefficient of  $x^7$  in the expansion of  $\left(3 + \frac{1}{x^3}\right)\left(2x^2 - \frac{1}{3x}\right)^5$ . [2]



- 5 (i) Find the equation of the normal to the curve  $y = \frac{1}{2}\ln(3x + 2)$  at the point  $P$  where  $x = -\frac{1}{3}$ . [4]

The normal to the curve at the point  $P$  intersects the  $y$ -axis at the point  $Q$ . The curve  $y = \frac{1}{2}\ln(3x + 2)$  intersects the  $y$ -axis at the point  $R$ .

- (ii) Find the area of the triangle  $PQR$ . [3]





- 6 (a) Matrices  $\mathbf{X}$ ,  $\mathbf{Y}$  and  $\mathbf{Z}$  are such that

$$\mathbf{X} = \begin{pmatrix} 2 & 3 \\ 4 & -1 \\ 6 & 5 \end{pmatrix}, \mathbf{Y} = (1 \quad -1 \quad 0) \quad \text{and} \quad \mathbf{Z} = \begin{pmatrix} 0 & -1 \\ 5 & 3 \end{pmatrix}.$$

Write down all the matrix products which are possible using any two of these matrices. Do not evaluate these products. [2]

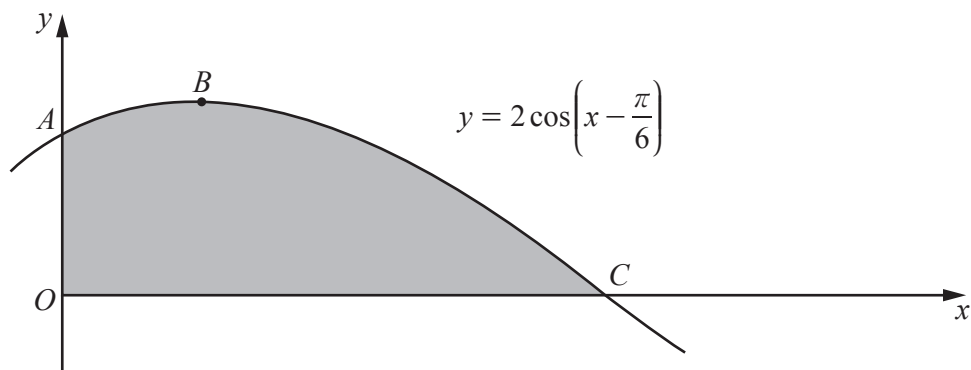
- (b) Matrices  $\mathbf{A}$ ,  $\mathbf{B}$  and  $\mathbf{C}$  are such that  $\mathbf{A} = \begin{pmatrix} 2 & -1 \\ 4 & 7 \end{pmatrix}$ ,  $\mathbf{B} = \begin{pmatrix} -4 & 2 \\ 10 & 4 \end{pmatrix}$  and  $\mathbf{AC} = \mathbf{B}$ .

- (i) Find  $\mathbf{A}^{-1}$ . [2]

- (ii) Hence find  $\mathbf{C}$ . [3]



7



The diagram shows part of the graph of  $y = 2 \cos\left(x - \frac{\pi}{6}\right)$ . The graph intersects the  $y$ -axis at the point  $A$ , has a maximum point at  $B$  and intersects the  $x$ -axis at the point  $C$ .

(i) Find the coordinates of  $A$ . [1]

(ii) Find the coordinates of  $B$ . [2]



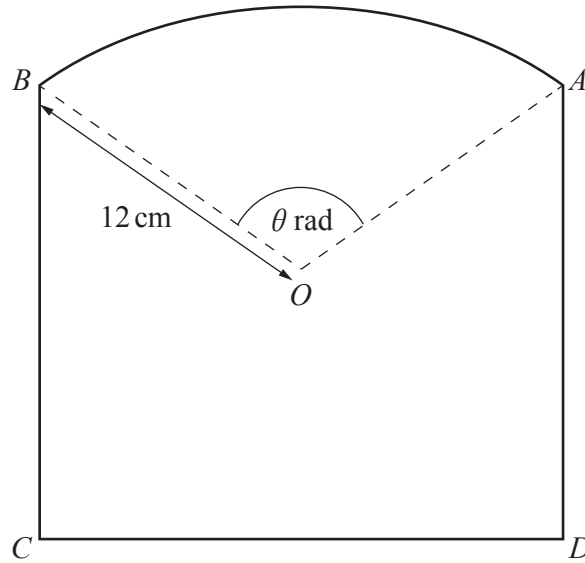
(iii) Find the coordinates of  $C$ . [2]

(iv) Find  $\int 2 \cos\left(x - \frac{\pi}{6}\right) dx$ . [1]

(v) Hence find the area of the shaded region. [2]

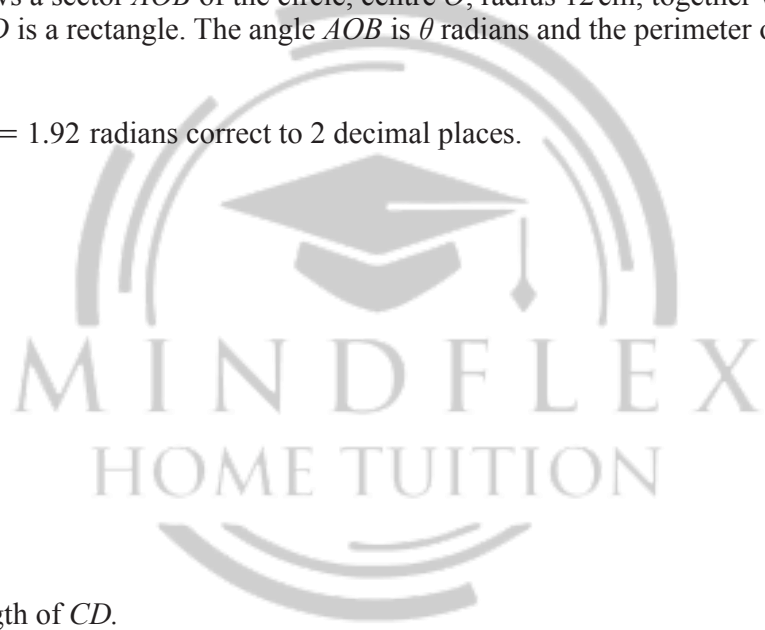


8



The diagram shows a sector  $AOB$  of the circle, centre  $O$ , radius  $12\text{ cm}$ , together with points  $C$  and  $D$  such that  $ABCD$  is a rectangle. The angle  $AOB$  is  $\theta$  radians and the perimeter of the sector  $AOB$  is  $47\text{ cm}$ .

- (i) Show that  $\theta = 1.92$  radians correct to 2 decimal places. [2]



- (ii) Find the length of  $CD$ . [2]

(iii) Given that the total area of the shape is  $425 \text{ cm}^2$ , find the length of  $AD$ .

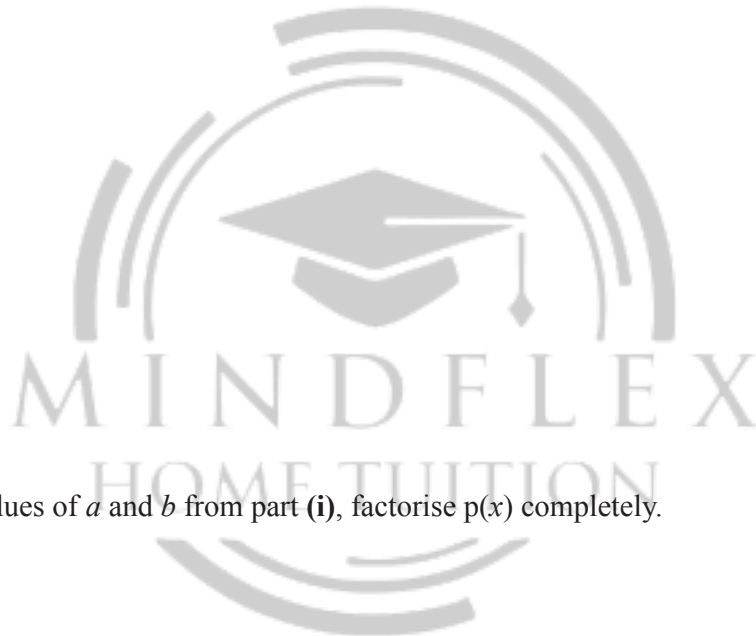
[5]



**9 Do not use a calculator in this question.**

The polynomial  $p(x)$  is  $ax^3 - 4x^2 + bx + 18$ . It is given that  $p(x)$  and  $p'(x)$  are both divisible by  $2x - 3$ .

(i) Show that  $a = 4$  and find the value of  $b$ . [4]



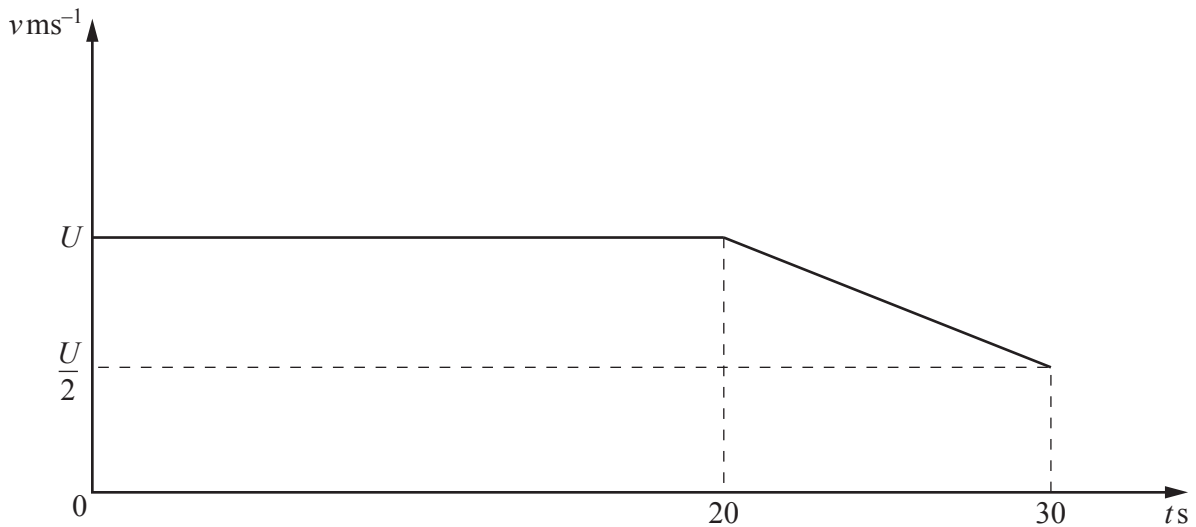
(ii) Using the values of  $a$  and  $b$  from part (i), factorise  $p(x)$  completely. [2]

(iii) Hence find the values of  $x$  for which  $p(x) = x + 2$  .

[3]



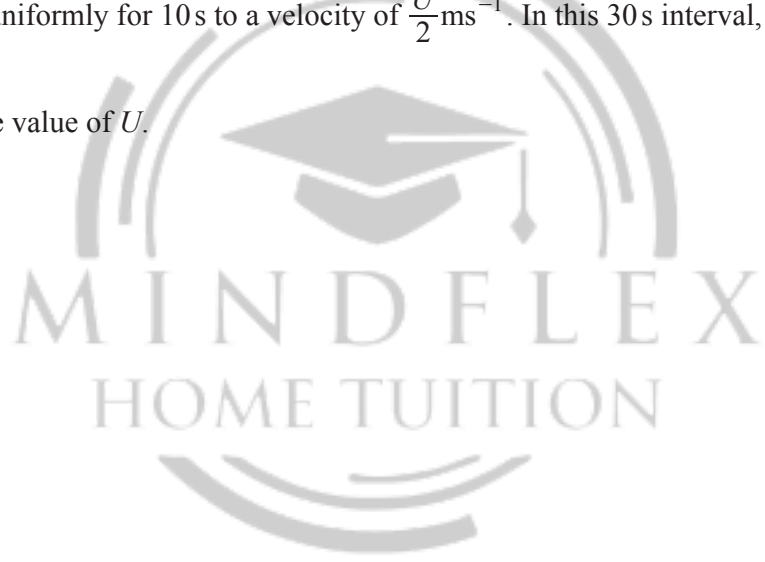
10 (a)



The diagram shows part of the velocity-time graph for a particle, moving at  $v \text{ ms}^{-1}$  in a straight line,  $t \text{ s}$  after passing through a fixed point. The particle travels at  $U \text{ ms}^{-1}$  for 20 s and then decelerates uniformly for 10 s to a velocity of  $\frac{U}{2} \text{ ms}^{-1}$ . In this 30 s interval, the particle travels 165 m.

(i) Find the value of  $U$ . [3]

(ii) Find the acceleration of the particle between  $t = 20$  and  $t = 30$ . [2]





(b) A particle  $P$  travels in a straight line such that,  $t$  s after passing through a fixed point  $O$ , its velocity,  $v \text{ ms}^{-1}$ , is given by  $v = \left( e^{\frac{t^2}{8}} - 4 \right)^3$ .

(i) Find the speed of  $P$  at  $O$ . [1]

(ii) Find the value of  $t$  for which  $P$  is instantaneously at rest. [2]

(iii) Find the acceleration of  $P$  when  $t = 1$ . [4]



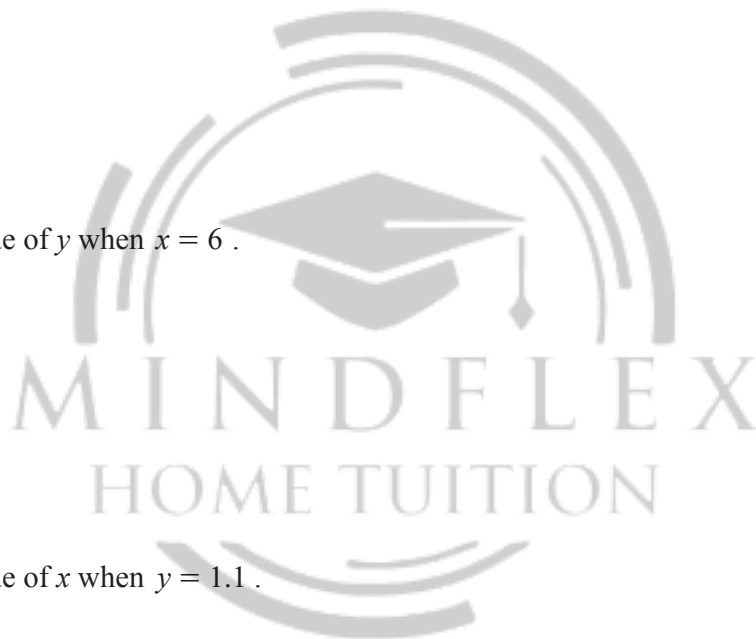
**Question 11 is printed on the next page.**

11 The variables  $x$  and  $y$  are such that when  $\ln y$  is plotted against  $x$ , a straight line graph is obtained. This line passes through the points  $x = 4, \ln y = 0.20$  and  $x = 12, \ln y = 0.08$ .

(i) Given that  $y = Ab^x$ , find the value of  $A$  and of  $b$ . [5]

(ii) Find the value of  $y$  when  $x = 6$ . [2]

(iii) Find the value of  $x$  when  $y = 1.1$ . [2]



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**ADDITIONAL MATHEMATICS**

**0606/11**

Paper 1

**October/November 2016**

MARK SCHEME

Maximum Mark: 80

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**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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<b>Page 2</b>	<b>Mark Scheme</b>	<b>Syllabus</b>	<b>Paper</b>
	<b>Cambridge IGCSE – October/November 2016</b>	<b>0606</b>	<b>11</b>

### Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

Question	Answer	Marks	Part Marks
<b>1 (a) (i)</b>	10	<b>B1</b>	
<b>(ii)</b>	22	<b>B1</b>	
<b>(iii)</b>	4	<b>B1</b>	
<b>(b) (i)</b>	$Q \subset R$	<b>B1</b>	
<b>(ii)</b>	$P \cap Q = \emptyset$ , or $\{ \}$	<b>B1</b>	
<b>2</b>	$a=1, b=-3, c=-1$	<b>B3</b>	<b>B1</b> for each
<b>3</b>	$3y^2 + 5y - 2 = 0$ $y = \frac{1}{3}, y = -2$ $x = 3^{\frac{1}{3}}, x = 3^{-2}$ $x = 1.44, x = \frac{1}{9}$	<b>B1, B1</b> <b>M1</b> <b>M1</b> <b>A1, A1</b>	<b>B1</b> for $5y$ or $5\log_3 x$ , <b>B1</b> for $-2$ for correct attempt at the solution of <i>their</i> quadratic equation for dealing with one base 3 logarithm correctly <b>A1</b> for each
<b>4 (i)</b>	$32x^{10} - \frac{80}{3}x^7 + \frac{80}{9}x^4$	<b>B3</b>	<b>B1</b> for each term, powers of $x$ must be simplified
<b>(ii)</b>	Coefficients needed: $\left(3 \times \text{their} - \frac{80}{3}\right) + (1 \times \text{their } 32)$ $= -48$	<b>M1</b> <b>A1</b>	for dealing with 2 terms Allow <b>A1</b> for $-48x^7$

Page 3	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Part Marks
5 (i)	$\frac{dy}{dx} = \frac{3}{2(3x+2)}$	<b>B1</b>	for correct derivative of log function
	When $x = -\frac{1}{3}$ , $y = 0$ , $\frac{dy}{dx} = \frac{3}{2}$	<b>B1</b>	for $y = 0$
	Equation of normal: $y = -\frac{2}{3}\left(x + \frac{1}{3}\right)$	<b>M1</b> <b>A1</b>	<b>M1</b> for attempt at a gradient of a perpendicular from differentiation and the equation of the normal
(ii)	$Q\left(0, -\frac{2}{9}\right)$ or $(0, 0.22)$ or better	<b>B1 ft</b>	Follow through on <i>their c</i> from part (i)
	$R\left(0, \frac{1}{2}\ln 2\right)$ or $(0, 0.35)$ or better	<b>B1</b>	
	Area of $PQR = \frac{1}{2}\left(\frac{1}{2}\ln 2 + \frac{2}{9}\right) \times \frac{1}{3}$ $= 0.0948$	<b>B1</b>	Allow 0.095
6 (a)	<b>YX, XZ</b>	<b>B2</b>	<b>B2</b> for both with no extras <b>B1</b> for 1 correct with or without extras <b>B1</b> for both correct with extras <b>B0</b> for anything else
(b) (i)	$\frac{1}{18}\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}$	<b>B1, B1</b>	<b>B1</b> for $\frac{1}{18}$ , <b>B1</b> for $\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}$
	(ii) $\mathbf{C} = \mathbf{A}^{-1}\mathbf{B}$ $= \frac{1}{18}\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}\begin{pmatrix} -4 & 2 \\ 10 & 4 \end{pmatrix}$ $= \begin{pmatrix} -1 & 1 \\ 2 & 0 \end{pmatrix}$	<b>M1</b> <b>A1, A1</b>	for pre-multiplication <b>A1</b> for any correct pair of elements, but must be from correct matrices

Page 4	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Part Marks
7	(i) $(0, \sqrt{3})$ or $(0, 1.73)$ or better	<b>B1</b>	
	(ii) $\left(\frac{\pi}{6}, 2\right)$ or $(0.524, 2)$ or better	<b>B1, B1</b>	<b>B1</b> for each
	(iii) $\cos\left(x - \frac{\pi}{6}\right) = 0$ $x = \frac{2\pi}{3}$ oe or 2.09 or better	<b>M1</b> <b>A1</b>	for correct attempt to solve trigonometric equation
	(iv) $2\sin\left(x - \frac{\pi}{6}\right)$ (+c)	<b>B1</b>	
	(v) Area = $\left[2\sin\left(x - \frac{\pi}{6}\right)\right]_0^{\frac{2\pi}{3}}$ = 2 + 1 = 3	<b>M1</b> <b>A1</b>	for correct use of <b>their</b> limits, in radians, into $k \sin\left(x - \frac{\pi}{6}\right)$ .
8	(i) $47 - 24 = 12\theta$ $\theta = \frac{23}{12}$ , so $\theta = 1.917$ or better $\theta = 1.92$ to 2dp	<b>M1</b> <b>A1</b>	for complete correct method to get $\theta =$ must have evidence of working to more than 2 dp, allow if 1.916 seen (truncated)
	(ii) $\sin \frac{\theta}{2} = \frac{CD/2}{12}$ $CD = \text{awrt } 19.6 \text{ or } 19.7$	<b>M1</b> <b>A1</b>	for a complete method, may use cosine rule to get $CD$
	(iii) Area of sector = awrt 138 Area of triangle $AOB$ = awrt 67 or 68 Area of segment = awrt 70 or 71  $AD \times AB + \text{segment area} = 425$ leading to $AD = \text{awrt } 18.1 \text{ or } 18.0$  <b>Alternative method:</b> Area of sector = awrt 138 Difference in length between $BC$ (or $AD$ ) and $OM$ where $M$ is the midpoint of $CD = 6.88$ , allow awrt 6.9 Remaining area consists of two trapezia each of width 9.85 and each of area 143.4 $\frac{1}{2}(2BC - 6.88) \times 9.85 = 143.4$ oe leading to $AD = \text{awrt } 18.1 \text{ or } 18.0$	<b>B1</b> <b>M1</b> <b>M1</b> <b>M1</b> <b>A1</b>  <b>B1</b> <b>M1</b> <b>M1</b> <b>M1</b> <b>A1</b>	for sector area, allow unsimplified for a correct attempt at area for segment area ( <i>their</i> sector area – <i>their</i> triangle area) for complete method to find $AD$ Allow <b>A1</b> for 18  for sector area for attempt to find difference between parallel sides  for area of one trapezium $\frac{1}{2}(2BC - \text{their } 6.88) \times \text{their } 9.85$ oe  for attempt to find either $BC$ or $AD$

Page 5	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Part Marks	
9 (i)	$p\left(\frac{3}{2}\right): \frac{27a}{8} - \left(4 \times \frac{9}{4}\right) + \frac{3b}{2} + 18 (=0)$	M1	for attempt at $p\left(\frac{3}{2}\right)$	
	$p'\left(\frac{3}{2}\right) = \left(3a \times \frac{9}{4}\right) - \left(8 \times \frac{3}{2}\right) + b (=0)$	M1	for differentiation and attempt at $p'\left(\frac{3}{2}\right)$	
	leading to $9a + 4b + 24 = 0$ oe and $27a + 4b - 48 = 0$ oe	M1	for solution of simultaneous equations, to get either $a$ or $b$	
	leading to $a = 4, b = -15$	A1	for both	
	(ii)	$(x+2)(2x-3)^2$ oe	M1, A1	M1 for attempt at long division or factorisation
	(iii)	$(x+2)(2x-3)^2 = x+2$ $x+2=0, x=-2$	B1	Must be using $(x+2)$ correctly using part (ii) to get $x=-2$
	$(2x-3)^2 = 1$ leading to $x=1, x=2$	M1 A1	for solution of the quadratic equation	
10 (a) (i)	$20U + \frac{1}{2}\left(U + \frac{U}{2}\right)10 = 165$	M1	for realising that area under the graph is needed and attempt to find an area	
	leading to $U = 6$	DM1	for equating their area to 165 and attempt to solve	
	(ii)	Gradient of line: $-0.3$	A1	
	(b) (i)	27	M1, A1	M1 for use of the gradient, must be negative
	(ii)	$t^2 = 8 \ln 4$ $t = 3.33$ or better	B1	
	(iii)	acceleration = $3 \frac{2t}{8} e^{\frac{t^2}{8}} \left( e^{\frac{t^2}{8}} - 4 \right)^2$	M1	for a correct attempt to solve $e^{\frac{t^2}{8}} = 4$
	When $t = 1, a = 6.98$	A1		
		M1, A1	M1 for a correct attempt to differentiate using the chain rule	
		M1, A1	M1 for use of $t = 1$ in their acceleration	

Page 6	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Part Marks
11 (i)	$\ln y = \ln A + x \ln b$	<b>B1</b>	may be implied, if equation not seen specifically, by correct values for $A$ and $b$
	Gradient: $\ln b = -\frac{0.12}{8}, = -0.015$	<b>M1</b>	for use of gradient to obtain $\ln b$
	$b = 0.985$	<b>A1</b>	Allow <b>A1</b> for $e^{-0.015}$
	Intercept: $\ln A = 0.26$	<b>DM1</b>	for use of one of the given points correctly
	$A = 1.30$	<b>A1</b>	Allow <b>A1</b> for $e^{0.26}$ or 1.3
	<b>Alternative 1</b>		
	$\ln y = \ln A + x \ln b$	<b>B1</b>	
	$0.2 = 4 \ln b + \ln A$	<b>M1</b>	for one correct equation
	$0.08 = 12 \ln b + \ln A$	<b>DM1</b>	for attempt to obtain either $\ln A$ or $\ln b$ from simultaneous equations
	$A = 1.30$ and $b = 0.985$	<b>A1, A1</b>	Allow <b>A1</b> for $b = e^{-0.015}$ and $a = e^{0.26}$ or 1.3
(ii)	<b>Alternative 2</b>		
	$1.22 = Ab^4$	<b>B1</b>	
	$1.08 = Ab^{12}$	<b>B1</b>	
		<b>M1</b>	for correct attempt to obtain $b$ or $A$ , must already have <b>B2</b>
	$A = 1.30$ and $b = 0.985$	<b>A1, A1</b>	Allow <b>A1</b> for $b = e^{-0.015}$ and $a = e^{0.26}$ or 1.3
	When $x = 6$ , $\ln y = 0.17$	<b>M1</b>	for $\ln y = \text{their } \ln A + 6 \text{ their } \ln b$ or $y = \text{their } A \times (\text{their } b)^6$
	$y = 1.19$	<b>A1</b>	allow awrt 1.18 to 1.20
	When $y = 1.1$ , $\ln y = 0.095$	<b>M1</b>	for $\ln 1.1 = \text{their } \ln A + x \text{ their } \ln b$ or $1.1 = \text{their } A \times (\text{their } b)^x$
	$x = 11$	<b>A1</b>	allow 10.5 to 11.5





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**ADDITIONAL MATHEMATICS**

**0606/21**

Paper 2

**October/November 2016**

**2 hours**

Candidates answer on the Question Paper.

Additional Materials: Electronic calculator

**READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

**DO NOT WRITE IN ANY BARCODES.**

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 80.

This document consists of **16** printed pages.

**Mathematical Formulae**

**1. ALGEBRA**

*Quadratic Equation*

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

*Binomial Theorem*

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1} b + \binom{n}{2} a^{n-2} b^2 + \dots + \binom{n}{r} a^{n-r} b^r + \dots + b^n,$$

where  $n$  is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

**2. TRIGONOMETRY**

*Identities*

$$\sin^2 A + \cos^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A$$

*Formulae for  $\triangle ABC$*

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2} bc \sin A$$

1 Solve the equation  $|4x - 3| = x$ . [3]

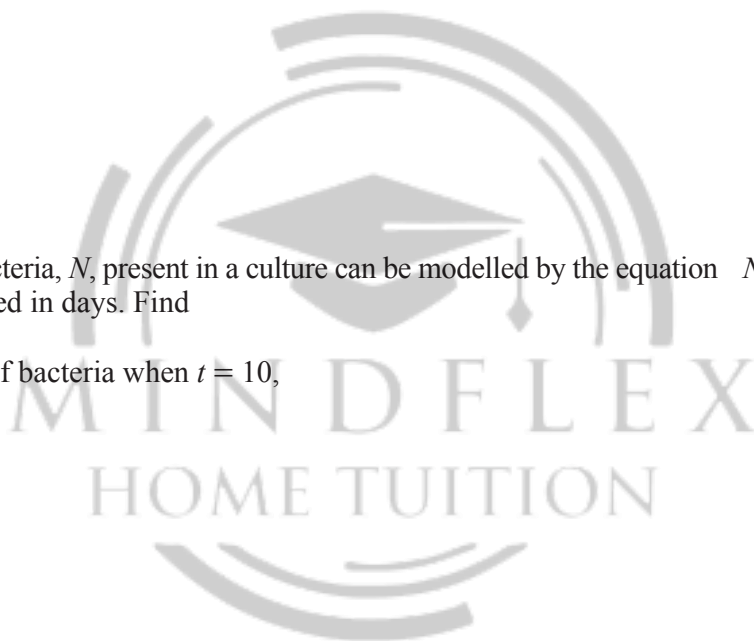
2 Without using a calculator, find the integers  $a$  and  $b$  such that  $\frac{a}{\sqrt{3}+1} + \frac{b}{\sqrt{3}-1} = \sqrt{3} - 3$ . [5]



3 Solve the equation  $2 \lg x - \lg\left(\frac{x+10}{2}\right) = 1$ . [5]

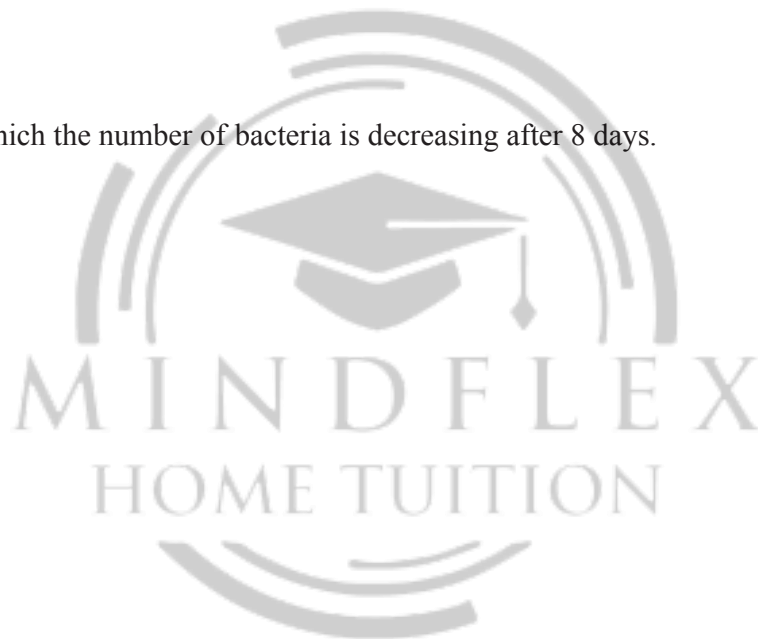
4 The number of bacteria,  $N$ , present in a culture can be modelled by the equation  $N = 7000 + 2000e^{-0.05t}$ , where  $t$  is measured in days. Find

(i) the number of bacteria when  $t = 10$ , [1]



(ii) the value of  $t$  when the number of bacteria reaches 7500, [3]

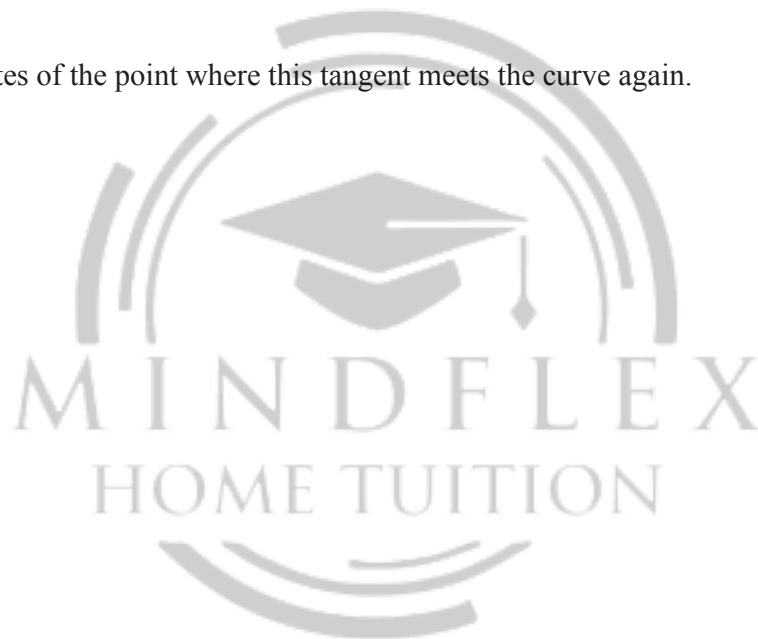
(iii) the rate at which the number of bacteria is decreasing after 8 days. [3]



5 The curve with equation  $y = x^3 + 2x^2 - 7x + 2$  passes through the point  $A (-2, 16)$ . Find

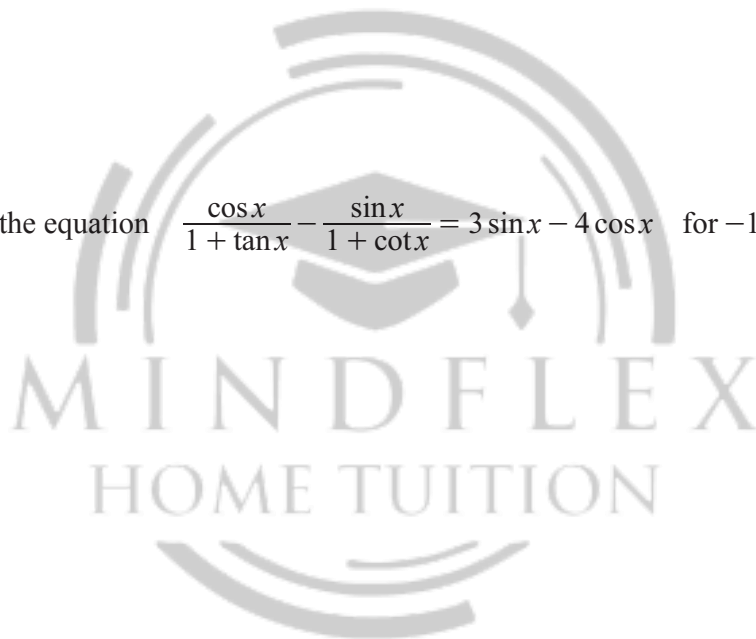
(i) the equation of the tangent to the curve at the point  $A$ , [3]

(ii) the coordinates of the point where this tangent meets the curve again. [5]

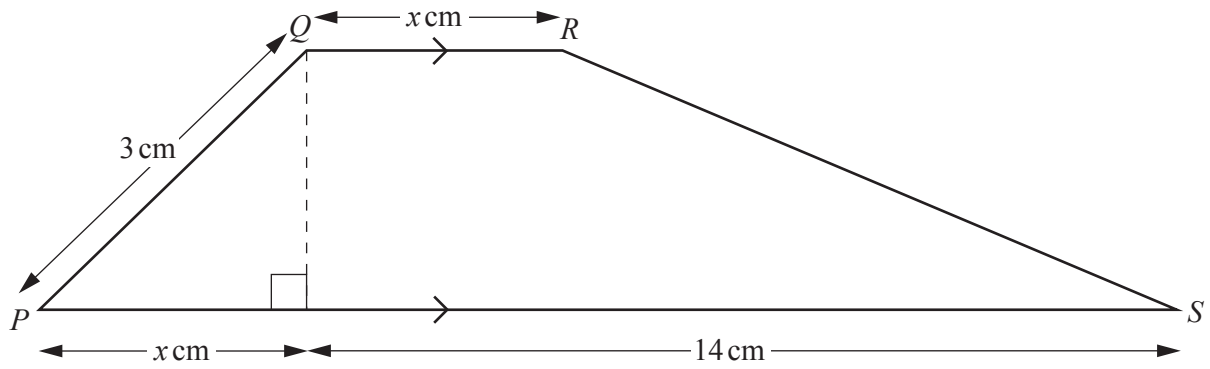


6 (i) Prove that  $\frac{\cos x}{1 + \tan x} - \frac{\sin x}{1 + \cot x} = \cos x - \sin x$ . [4]

(ii) Hence solve the equation  $\frac{\cos x}{1 + \tan x} - \frac{\sin x}{1 + \cot x} = 3 \sin x - 4 \cos x$  for  $-180^\circ < x < 180^\circ$ . [4]



7



- (i) Show that the area,  $A \text{ cm}^2$ , of the trapezium  $PQRS$  is given by  $A = (7 + x)\sqrt{9 - x^2}$ . [2]





(ii) Given that  $x$  can vary, find the stationary value of  $A$ .

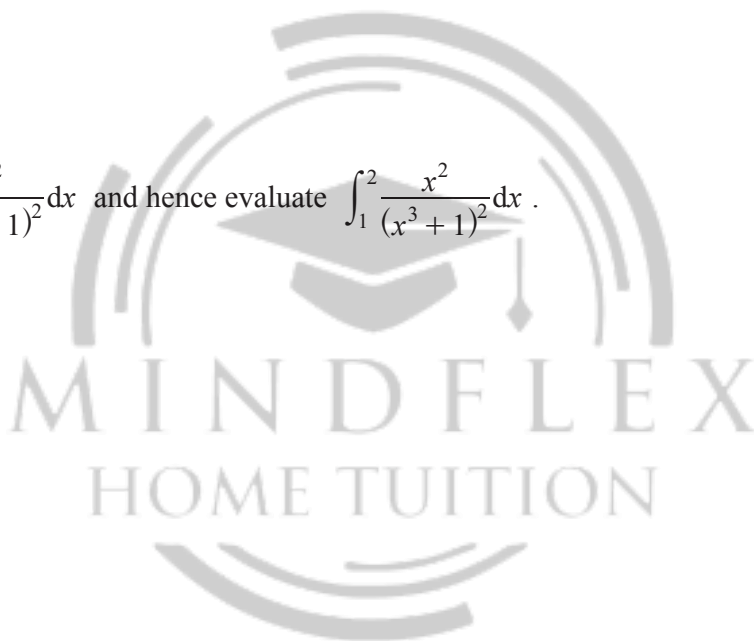
[7]



8 The function  $f(x)$  is given by  $f(x) = \frac{3x^3 - 1}{x^3 + 1}$  for  $0 \leq x \leq 3$ .

(i) Show that  $f'(x) = \frac{kx^2}{(x^3 + 1)^2}$ , where  $k$  is a constant to be determined. [3]

(ii) Find  $\int \frac{x^2}{(x^3 + 1)^2} dx$  and hence evaluate  $\int_1^2 \frac{x^2}{(x^3 + 1)^2} dx$ . [4]



(iii) Find  $f^{-1}(x)$ , stating its domain.

[4]



- 9 The line  $y = kx - 4$ , where  $k$  is a positive constant, passes through the point  $P(0, -4)$  and is a tangent to the curve  $x^2 + y^2 - 2y = 8$  at the point  $T$ . Find
- (i) the value of  $k$ , [5]



(ii) the coordinates of  $T$ ,

[3]

(iii) the length of  $TP$ .

[2]



- 10 The town of Cambley is 5 km east and  $p$  km north of Edwintown so that the position vector of Cambley from Edwintown is  $\begin{pmatrix} 5000 \\ 1000p \end{pmatrix}$  metres. Manjit sets out from Edwintown at the same time as Raj sets out from Cambley. Manjit sets out from Edwintown on a bearing of  $020^\circ$  at a speed of  $2.5 \text{ ms}^{-1}$  so that her position vector relative to Edwintown after  $t$  seconds is given by  $\begin{pmatrix} 2.5t \cos 70^\circ \\ 2.5t \cos 20^\circ \end{pmatrix}$  metres. Raj sets out from Cambley on a bearing of  $310^\circ$  at  $2 \text{ ms}^{-1}$ .

(i) Find the position vector of Raj relative to Edwintown after  $t$  seconds. [2]



Manjit and Raj meet after  $T$  seconds.

(ii) Find the value of  $T$  and of  $p$ .

[5]



**Question 11 is printed on the next page.**

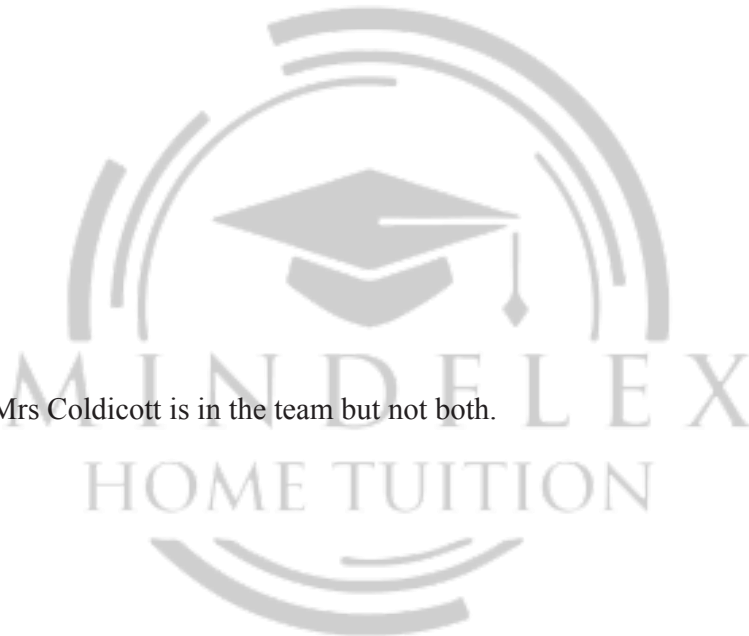
- 11 Mr and Mrs Coldicott have 5 sons and 4 daughters. All 11 members of the family play tennis. Six members of the family enter a tennis competition where teams consist of 4 males and 2 females.

Find the number of different teams of 4 males and 2 females that could be selected if

- (i) there are no further restrictions, [2]

- (ii) Mr and Mrs Coldicott must both be in the team, [2]

- (iii) either Mr or Mrs Coldicott is in the team but not both. [3]



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**Cambridge International Examinations**  
Cambridge International General Certificate of Secondary Education

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**ADDITIONAL MATHEMATICS**

**0606/21**

Paper 2

**October/November 2016**

MARK SCHEME

Maximum Mark: 80

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**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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### Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

Question	Answer	Marks	Part Marks
<b>1</b>	$4x - 3 = x \rightarrow x = 1$ $4x - 3 = -x$ $x = 0.6$  <b>OR</b> $(4x - 3)^2 = x^2$ $15x^2 - 24x + 9 = 0$ $3(x - 1)(5x - 3) = 0$ $x = 1$ and $x = 0.6$	<b>B1</b> <b>M1</b> <b>A1</b>  <b>B1</b> <b>M1</b> <b>A1</b>	www use of $-x$ or $-(4x - 3)$ but not both.  solve correct 3 term quadratic www
<b>2</b>	$a(\sqrt{3} - 1) + b(\sqrt{3} + 1)$ $= (\sqrt{3} - 3)(\sqrt{3} - 1)(\sqrt{3} + 1)$ $= 2(\sqrt{3} - 3)$ oe  $a + b = 2$ $-a + b = -6$  $b = -2$ and $a = 4$	<b>M1</b>  <b>DM1</b> <b>A1</b> <b>DM1</b> <b>A1</b>	Common denominator or $\times (\sqrt{3} - 1)(\sqrt{3} + 1)$  equate constant terms and $\sqrt{3}$ terms. both correct solve two <b>linear</b> equations to obtain $a =$ or $b =$ both correct
<b>3</b>	$2\lg x = \lg x^2$ $1 = \lg 10$  $\lg x^2 - \lg \left( \frac{x + 10}{2} \right) = \lg \left( \frac{2x^2}{x + 10} \right)$ oe  $2x^2 - 10x - 100 = 0 \rightarrow 2(x + 5)(x - 10) = 0$  $x = 10$ only	<b>B1</b> <b>B1</b>  <b>B1</b> <b>M1</b> <b>A1</b>	soi anywhere soi anywhere  soi division; logs may be removed  obtain correct 3 term quadratic equation and attempt to solve $x = -5$ must not remain.

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Question	Answer	Marks	Part Marks
4 (i)	$t = 10 \rightarrow N = 7000 + 2000e^{-0.5}$ $= 8213$ or 8210	<b>B1</b>	Do not accept non integer responses.
(ii)	$N = 7500 \rightarrow 7500 = 7000 + 2000e^{-0.05t}$ $e^{-0.05t} = \frac{500}{2000}$ $-0.05t = \ln 0.25 \rightarrow t = \frac{\ln 0.25}{-0.05}$ $= 27.7$ (days)	<b>M1</b> <b>M1</b> <b>A1</b>	insert and make $e^{-0.05t}$ subject  take logs and make $t$ the subject awrt 27.7
(iii)	$\frac{dN}{dt} = -100e^{-0.05t}$ $t = 8 \rightarrow \frac{dN}{dt} = \pm 67$ (.0)	<b>M1</b> <b>A1</b> <b>A1</b>	$ke^{-0.05t}$ where $k$ is a constant $k = -100$ or $-0.05 \times 2000$ awrt $\pm 67$ mark final answer
5 (i)	$\frac{dy}{dx} = 3x^2 + 4x - 7$ $x = -2 \rightarrow \frac{dy}{dx} = 12 - 8 - 7 = -3$ Equation of tangent : $\frac{y-16}{x+2} = -3 \rightarrow y = -3x + 10$	<b>B1</b> <b>M1</b> <b>A1</b>	insert $x = -2$ into <i>their</i> gradient and use $(-2, 16)$ and <i>their</i> gradient of tangent in equation of line.
(ii)	Tangent cuts curve again $x^3 + 2x^2 - 7x + 2 = -3x + 10$ $x^3 + 2x^2 - 4x - 8 = 0$ $(x+2)(x+2)(x-2) = 0$ $x = 2, y = 4$	<b>M1</b> <b>A1</b> <b>M1</b> <b>A1A1</b>	equate curve and <i>their</i> linear answer from (i).  factorise: $(x \pm 2)$ and a two or three term quadratic is sufficient. Allow long division withhold final <b>A1</b> if $(2, 4)$ not clearly identified as their sole answer.
6 (i)	$\frac{\cos x}{1 + \tan x} - \frac{\sin x}{1 + \cot x} = \frac{\cos x}{1 + \frac{\sin x}{\cos x}} - \frac{\sin x}{1 + \frac{\cos x}{\sin x}}$ $= \frac{\cos^2 x}{\cos x + \sin x} - \frac{\sin^2 x}{\cos x + \sin x}$ $= \frac{(\cos x - \sin x)(\cos x + \sin x)}{(\cos x + \sin x)}$	<b>M1</b> <b>M1</b> <b>A1</b> <b>A1</b>	$\tan x = \frac{\sin x}{\cos x}$ and $\cot x = \frac{\cos x}{\sin x}$  Attempt to multiply by $\cos x$ and $\sin x$  AG
(ii)	$-\sin x + \cos x = 3\sin x - 4\cos x$ $5\cos x = 4\sin x$ $\tan x = \frac{5}{4}$ $x = 51.3^\circ, -128.7^\circ$	<b>M1</b> <b>A1</b> <b>A1A1</b>	equate and collect $\sin x$ and $\cos x$ oe  <b>FT</b> from $\tan x = k$

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Question	Answer	Marks	Part Marks
7 (i)	$h = \sqrt{9 - x^2}$ $A = \frac{\sqrt{9 - x^2}}{2}(14 + x + x) = \sqrt{9 - x^2}(7 + x)$	<b>B2/1/0</b>	Must be clear that $\sqrt{9 - x^2}$ is the height of the trapezium. $14 + 2x$ oe must be seen AG
(ii)	$\frac{dA}{dx} = \sqrt{9 - x^2} + (7 + x) \frac{1}{2}(9 - x^2)^{-0.5} \times -2x$ $\frac{dA}{dx} = 0 \rightarrow 9 - x^2 = 7x + x^2$ $2x^2 + 7x - 9 = 0$ $x = 1$ $A = 16\sqrt{2}$ or $8\sqrt{8}$ or $\sqrt{512}$ or 22.6	<b>M1</b> <b>A2/1/0</b>  <b>M1</b> <b>A1</b>  <b>A1</b> <b>A1</b>	product rule on correct function minus 1 each error, allow unsimplified.  equate to 0 and simplify to a linear or quadratic equation. correct three term quadratic obtained  Extra positive answer loses penultimate <b>A1</b> . ignore negative solution.
8 (i)	$f'(x) = \frac{(x^3 + 1)9x^2 - (3x^3 - 1)3x^2}{(x^3 + 1)^2}$ $= \frac{12x^2}{(x^3 + 1)^2}$	<b>M1</b> <b>A1</b>  <b>A1</b>	quotient rule or product rule all correct  www beware $9x^6 - 9x^6$ gets <b>A0</b>
(ii)	$\int_1^2 \frac{x^2}{(x^3 + 1)^2} dx = \frac{1}{12} \left[ \frac{3x^3 - 1}{x^3 + 1} \right]_1^2$ $= \frac{1}{12} \left[ \frac{23}{9} - \frac{2}{2} \right]$ $= \frac{7}{54}$	<b>M1</b> <b>A1</b>  <b>DM1</b>  <b>A1</b>	$c \times \frac{3x^3 - 1}{x^3 + 1}$ <b>FT</b> $c = \frac{1}{\text{their}12}$  top limit – bottom limit in <i>their</i> integral.  or 0.130 or 0.1296 or 0.12
(iii)	$x = \frac{3y^3 - 1}{y^3 + 1}$ $y^3 = \frac{x + 1}{3 - x}$ $f^{-1}(x) = \sqrt[3]{\frac{x + 1}{3 - x}}$ Domain : $-1 \leq x \leq 2\frac{6}{7}$	<b>B1</b>   <b>B1</b> <b>B1</b> <b>B1</b>	make $y^3$ or $x^3$ the subject  <b>FT</b> take cube root (as long as $y^3$ or $x^3$ equals a fraction with terms in $x$ or $y$ only) oe <b>FT</b> change $x$ and $y$ – can be done at any time Allow upper limit of 2.86. Do not isw

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Question	Answer	Marks	Part Marks
9	(i) tangent touches circle $x^2 + (kx - 4)^2 - 2(kx - 4) = 8$ $k^2x^2 + x^2 - 8kx - 2kx + 16 = 0$ or better Equal roots as tangent touches circle : $b^2 = 4ac$ $(-10k)^2 = 4(k^2 + 1) \times 16$ $36k^2 = 64$ $k = +\frac{4}{3}$ only	M1 A1 DM1 A1 A1	eliminate $y$ or $x$ allow unsimplified use of discriminant on 3 term quadratic soi oe any inequality loses last A1
	(ii) $x = \frac{-b}{2a} \rightarrow x = \frac{\frac{4}{3} \times 10}{\frac{25}{9}}$ $x = \frac{12}{5} \quad y = -\frac{4}{5}$ OR tangent $y = \frac{4}{3}x - 4$ cuts radius $y = -\frac{3}{4}x + 1$ at $x = \frac{12}{5}$ $y = -\frac{4}{5}$	M1 A1A1 M1 A1	use $x = \frac{-b}{2a}$ find equation of radius and attempt to solve with tangent
	OR Obtain $25x^2 - 120x + 144 = 0$ oe $(5x - 12)(5x - 12) = 0$ $x = \frac{12}{5} \rightarrow y = -\frac{4}{5}$	M1 A1A1	obtain any 3 term quadratic using <i>their</i> non zero $k$ and reach $x = \dots$
	(iii) $TP = \sqrt{(0 - 2.4)^2 + (-4 + 0.8)^2} = 4$	M1A1	M1 for using <i>their</i> $T$ and $(0, -4)$ . Signs must be correct.

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Question	Answer	Marks	Part Marks
10 (i)	$r_j = \begin{pmatrix} 5000 \\ 1000p \end{pmatrix} + \begin{pmatrix} -2\cos 40 \\ 2\cos 50 \end{pmatrix} t$	B1 B1	x coordinate oe y coordinate oe
(ii)	$2.5t\cos 70 = 5000 - 2t\cos 40$ $t = \frac{5000}{2.5\cos 70 + 2\cos 40}$ $= 2095$ awrt or 2090 or 2100 $(2.5\cos 20 - 2\cos 50) \times 2095 = 1000p$ $p = 2.23$ awrt	M1 DM1 A1 M1 A1	equate <i>their</i> x values (must be 3 terms) make <i>t</i> the subject allow one sign error equate <i>their</i> y values (must be 3 terms) and insert <i>their</i> <i>t</i> or $ t $ .
11 (i)	Free choice : no. of ways ${}^6C_4 \times {}^5C_2 = 15 \times 10$ $= 150$	B1 B1	${}^6C_4 \times$ another ${}^nC_r$ term only $\times {}^5C_2$ and answer or vice versa
(ii)	Both Mr and Mrs Coldicott ${}^5C_3 \times {}^4C_1 = 10 \times 4$ $= 40$	B1 B1	${}^5C_3 \times$ another ${}^nC_r$ term only $\times {}^4C_1$ and answer or vice versa
(iii)	Mr C and not Mrs C ${}^5C_3 \times {}^4C_2 (= 60)$ Not Mr C and Mrs C ${}^5C_4 \times {}^4C_1 (= 20)$ Total = 80  OR Total = (i) – (ii) – neither Neither = ${}^5C_4 \times {}^4C_2 = 30$ Total = $150 - 40 - 30 = 80$	B1 B1 B1 M1 A1 A1	An incorrect final answer does not affect the awarding of the first two B1 marks.  www